

దినాంళ : 21. 06. 2018 ]
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## General Instructions to the Candidate :

1. This Question Paper consists of 50 objective and subjective types of questions.
2. This question paper has been sealed by reverse jacket. You have to cut on the right side to open the paper at the time of commencement of the examination. Check whether all the pages of the question paper are intact.
3. Follow the instructions given against both the objective and subjective types of questions.
4. Figures in the right hand margin indicate maximum marks for the questions.
5. The maximum time to answer the paper is given at the top of the question paper. It includes 15 minutes for reading the question paper.
I. Four alternatives are given for each of the following questions / incomplete statements. Only one of them is correct or most appropriate. Choose the correct alternative and write the complete answer along with its letter of alphabet.

$$
8 \times 1=8
$$

1. $\quad A$ and $B$ are two sets, such that $n(A)=37, n(B)=26$ and $n(A \cup B)=51$; then $n(A \cap B)$ is
(A) 12
(B) 63
(C) 14
(D) 25
2. Geometric mean between $\frac{1}{2}$ and $\frac{1}{8}$ is
(A) 16
(B) $\frac{1}{16}$
(C) $\frac{1}{4}$
(D) 4
3. HCF of any two prime numbers is
(A) a prime number
(B) a composite number
(C) an odd number
(D) an even number
4. If $f(x)=2 x^{3}+3 x^{2}-11 x+6$ then the value of $f(-1)$ is
(A) 0
(B) -10
(C) -18
(D) 18
5. In $\triangle A B C, \mid A B C=90^{\circ}, B D \perp A C$ if $B D=8 \mathrm{~cm}$ and $A D=4 \mathrm{~cm}$ then the length of $C D$ is

(A) 16 cm
(B) 4 cm
(C) 64 cm
(D) 12 cm
6. $\frac{\sin \left(90^{\circ}-\theta\right)}{\cos \left(90^{\circ}-\theta\right)}$ where ' $\theta$ ' is acute, is equal to
(A) $\sec \theta$
(B) $\cot \theta$
(C) $\tan \theta$
(D) $\operatorname{cosec} \theta$
7. The co-ordinates of the mid-point of the line segment joining the points $(2,3)$ and (4, 7 ) are
(A) $(-3,-5)$
(B) $(1,2)$
(C) $(3,5)$
(D) $(6,10)$
8. Formula used to find the surface area of a sphere whose radius ' $r$ ' units is
(A) $\pi r^{2}$
(B) $2 \pi r^{2}$
(C) $3 \pi r^{2}$
(D) $4 \pi r^{2}$
II. Answer the following :
9. A boy has 2 pants and 4 shirts. How many different pairs of a pant and a shirt can he dress up with ?
10. Write sample space for the random experiment 'tossing two fair coins simultaneously once'.
11. The given pie chart shows the annual agricultural yield of different crops in a certain place. If the total production is 3600 tons, what is the yield of Ragi in tons ?


PR (D)-60008
12. If $(x+3)$ is one of the factor of $f(x)=x^{2}+5 x+6$, find the other factor.
13. What are concentric circles ?
14. Two straight lines are perpendicular to each other. If the slope of one line is $\frac{1}{\sqrt{3}}$, find the slope of the other line.
III. 15. If $A=\{1,2,3\}$ and $B=\{2,3,4,5\}$ are the subsets of $U=\{1,2,3,4,5,6,7,8\}$, verify $(A \cap B)^{\prime}=A^{\prime} \cup B^{\prime}$.
16. Find the sum of infinite terms of the geometric series $2+\frac{2}{3}+\frac{2}{9}+\ldots .$.
17. Prove that $2+\sqrt{3}$ is an irrational number.
18. Find the number of diagonals that can be drawn in an octagon.
19. Find the sum of all two digit natural numbers which are divisible by 5 .
20. Find how many 4 digit numbers can be formed by using the digits $1,2,3$, 4, 5 without repetition ? How many of these are less than 2000 ?

If $2\left({ }^{n} P_{2}\right)+50={ }^{2 n} P_{2}$, find the value of $n$.
21. Two unbiased dice whose faces are numbered 1 to 6 are rolled once. Find the probability of getting a sum equal to 7 on their top faces.
22. Rationalise the denominator and simplify :

$$
\frac{3 \sqrt{2}}{\sqrt{5}-\sqrt{2}}
$$

23. Simplify $(\sqrt{75}-\sqrt{45})(\sqrt{20}+\sqrt{12})$.
24. Find the quotient and remainder by using synthetic division :

$$
\left(3 x^{3}-2 x^{2}+7 x-5\right) \div(x-3)
$$



Verify whether $(x-2)$ is a factor of $f(x)=x^{3}-3 x^{2}+6 x-20$ by using factor theorem.
25. In $\triangle A B C, D E \| B C$, if $A D=2 \mathrm{~cm}, D B=5 \mathrm{~cm}$ and $A E=4 \mathrm{~cm}$, find $A C$.

26. Draw a circle of radius 4.5 cm and a chord $P Q$ of length 7 cm in it. Construct a tangent at $P$.
27. Find the distance between the co-ordinates of the points (2, 4 ) and $(8,12)$ by using distance formula.
28. In a hockey match team ' $A$ ' scored one goal less than twice the number of goals scored by team ' $B$ '. If the product of the number of goals scored by both the teams is 15 , find the number of goals scored by each team.
29. In the given $\triangle A B C$, ' $\theta$ ' is acute. Write the values of the following trigonometric ratios related to $\theta$ :
(a) $\sin \theta$
(b) $\cos \theta$
(c) $\operatorname{cosec} \theta$
(d) $\sec \theta$.

30. Draw a plan by using the information given below :
( Scale 20 metres $=1 \mathrm{~cm}$ )

|  | Metre to C |  |
| :---: | :---: | :---: |
|  | 140 |  |
| 80 to D | 90 |  |
| 30 to E | 60 | 60 to B |
|  | 20 |  |
|  | From A |  |

31. If $P=\{1,2,3,4\}, Q=\{2,3,4,5,6\}$ are the subsets of
$U=\{1,2,3,4,5,6,7,8,9,10\}$, then draw Venn diagram to represent $(P \cup Q)^{\prime}$.
32. Write the formula used to find the following :
(a) Sum of first ' $n$ ' natural numbers
(b) Harmonic mean between $a$ and $b(a>b)$.
33. Write the values of the following :
(a) ${ }^{100} P_{0}$
(b) ${ }^{10} C_{1}$.
34. Draw a pie chart to represent the survey carried out in the class regarding places of visit for excursion and the number of students who opted each place.

| Places | Mysuru | Vijayapura | Gokorna | Chitradurga |
| :---: | :---: | :---: | :---: | :---: |
| Number of students | 14 | 6 | 2 | 18 |

35. Find the product of $\sqrt[3]{2}$ and $\sqrt[4]{3}$.
36. Determine the nature of the roots of the equation $2 x^{2}-5 x-1=0$.
37. In Rhombus $A B C D$, prove that $4 A B^{2}=A C^{2}+B D^{2}$.

38. Find the remainder when $P(x)=x^{3}+3 x^{2}-5 x+8$ is divided by $(x-3)$ by remainder theorem.
39. Find the distance between origin and the point ( $-8,15$ ).
40. If $\cos \theta=\frac{5}{13}$, find the value of $\frac{\sin \theta+\cos \theta}{\sin \theta-\cos \theta}$.
IV. 41. In a harmonic progression 5 th term is $\frac{1}{12}$ and 11 th term is $\frac{1}{15}$. Find its 25th term.

## OR

If the third term of a geometric progression is 12 and its sixth term is 96, find the sum of first 9 terms.
42. Calculate the variance of the following data:

| Class-interval | $0-4$ | $5-9$ | $10-14$ | $15-19$ | $20-24$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency $(f)$ | 1 | 2 | 5 | 4 | 3 |

43. Solve $(2 x+3)(3 x-2)+2=0$ by using formula.

OR

If one root of the equation $x^{2}+p x+q=0$ is four times the other, prove that $4 p^{2}-25 q=0$.
44. Prove that "The tangents drawn from an external point to a circle are equal".
45. In $\triangle A B C, A B=A C$. $P$ is a point on $B C$ such that $P N \perp A C$ and $P M \perp A B$ as shown in the figure. Prove that $\overline{M B} \cdot \overline{C P}=\overline{N C} \cdot \overline{B P}$.


OR

In $\triangle A B C, D E \| B C$. If $3 D E=2 B C$ and the area of $\triangle A B C$ is $81 \mathrm{~cm}^{2}$, show that the area of $\triangle A D E$ is $36 \mathrm{~cm}^{2}$.

46. Prove that $(1+\cot A-\operatorname{cosec} A)(1+\tan A+\sec A)=2$.

OR

From the top of a building 20 m high, the angle of elevation of the top of a vertical pole is $30^{\circ}$ and the angle of depression of the foot of the same pole is $60^{\circ}$. Find the height of the pole.
V. 47. Solve the equation $x^{2}+x-6=0$ graphically. 4
48. Construct a direct common tangent to two circles of radii 4 cm and 2 cm whose centres are 9 cm apart. Measure and write the length of the direct common tangent.
49. Prove that "In a right angled triangle, square on the hypotenuse is equal to sum of the squares on the other two sides".
50. A solid is in the shape of a cylinder with a cone attached at one end and a hemisphere attached to the other end as shown in the figure. All of them are of the same radius 7 cm . If the total length of the solid is 61 cm and height of the cylinder is 30 cm , calculate the cost of painting the outer surface of the solid at the rate of Rs. 10 per $100 \mathrm{~cm}^{2}$.


OR

PR (D)-60008

A solid metallic cylinder of diameter 12 cm and height 15 cm is melted and recast into toys in the shape of right circular cone mounted on a hemisphere as shown in the figure. If radii of the cone and hemisphere are each equal to 3 cm and the height of the toy is 7 cm , calculate the number of such toys that can be formed.


